Dynamics of motor vehicle equipped with post-impact control system to avoid other road accidents

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Abstract

The paper presents elements related to the dynamics of the vehicle equipped with a post-impact dynamics control system, so if a first impact has occurred. Possible solutions are given in practice. A mathematical model used for the post-impact control system is presented. A real operational accident is targeted, through the comparative study in case of lack and in case of existence of a post-impact control system.

Keywords: Electronic control; ABS; ESC; ESP; PISC

1. Introduction

From the practice of operating vehicles, it was found that of the total number of road accidents approximately 25% are multiple, so involving more than two vehicles; for example, there are situations with collisions of three vehicles, or two vehicles and a fixed obstacle (wall, tree etc.). It is therefore of practical interest to have solutions to avoid other collisions after a first impact has already taken place; thus, the need for post-impact displacement control systems arose [1, 3, 7, 8, 9, 10, 12].

For example, Figure 1 shows the actual operating case of a multiple impact with three vehicles marked V1, V2, V3. This is case no. 2009-09-088 to NASS-CDS (National Automotive Sampling System - Crashworthiness Data System); it was estimated that if the V2 vehicle had a post-impact control system, the last two collisions would not have occurred (Impact 2 and Impact 3).

As a real world example, Figure 1 shows a crash which depicts devastating multi-impact consequences after a minor initial impact. The three vehicles involved were traveling in the same direction before the crash. Vehicle 1 (V1) and vehicle 3 (V3) illustrate different trucks, and vehicle 2 (V2) is a passenger car which had multiple impacts. Vehicles depicted with dotted lines represent moving state and vehicles with solid lines represent stopped state. The first event started when V1 changed lanes. The driver of V1 might not have realized the existence of V2, and the right front corner of V1 came in contact with the left rear corner of V2. Then, V2 spun counter-clockwise and began crossing lanes to the left until V2’s left front side came in contact with a metal guardrail, causing Event 2. After that, V2 spun clockwise and crossed lanes to the right. Finally, in Event 3, V2’s right side struck the left rear tires of V3’s trailer. The passenger in V2 suffered severe injuries. As imagined from the picture at each event, the first impact for V2 was relatively minor structural deformation, and severities were much higher in subsequent impacts [6].

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2. Theoretical aspects

Post-impact displacement control can be performed with the following solutions:

Solution 1: by additional braking of the vehicle immediately after its first impact, in which case the ABS and ESC systems are used. In practice, the systems called MCB: Multi-Collision Brake (Porsche, Volkswagen - figure 2a, Skoda - figure 2b, Seat etc.), or SCBA: Secondary Collision Brake Assist (Audi), Post-Crash-iBrake (BMW) etc.

Therefore, in this solution, the control system has the role of avoiding a second impact by additional braking, when the vehicle has previously been involved in a collision. On first impact, if the airbag has been deployed, information is transmitted from its microcontroller to the electronic ESC stability control system to brake the vehicle using ABS. If the braking system is intact after the first impact, then it will brake the vehicle automatically. This additional braking reaches a speed of 10 km/h in a maximum of 6 milliseconds, which allows either the avoidance of the second impact or the reduction of its effects if it still occurs.

As it turns out, the MCB system acts independently of the driver, who is often not even able to control the vehicle after the first impact. It should also be noted that, even after a first impact, the microcontroller of the ESC stability control system can ensure the braking of a pair of opposite front and rear wheels, a facility provided by design and construction.

Solution 2: by braking and steering immediately after a first impact, in which case the facilities offered by the ABS (Anti-Lock Braking System), ESC/ESP (Electronic Stability Control / Electronic Stability Program) and PISC (Post-Impact Stability Control) functions are used, as shown in figure 3 [4, 5, 15].
As can be seen in Figure 3, the inlet variables for the ABS system are the brake pressure controlled by the ESC, the required slip and their actual slip; the output parameter is the braking pressure on all four wheels. The input variables of the ESC are the steering angle and the state quantities of the system, the last being the longitudinal speed, the lateral speed, the angular speed of rotation of the vehicle; the output parameters are the braking pressure and the required slip of the four wheels. The input variables of the PISC are the state values of the system, and the output variables are the steering angle and the braking pressure.

In Figure 3 there is also the estimator of the state variables of the system, which establishes the mentioned variables based on the information provided from the built-in transducers, radars and video cameras that serve to identify fixed or mobile obstacles that can generate a second impact. The additional brake actuation is similar to the previous solution, and the steering actuation is similar to the EPAS (Electric Power Assisted Steering) steering system.

Solution 3: by accelerating the vehicle after the primary impact, in order to avoid a secondary collision with another moving vehicle. In this case the post-impact control system takes into account the distances and the relative speed between the two vehicles and applies a certain movement pattern in traffic.

Solution 4: by optimally controlling the movement of the vehicle, to establish its trajectory in order to avoid a secondary collision. This solution uses a mathematical model of vehicle dynamics (presented below), based on which the impact forces at the first collision and the optimal steering angle are established to avoid secondary impact.

3. The mathematical model of the vehicle dynamics

The most used mathematical model is the one with 4 degrees of freedom, whose schemes are presented in figure 4. The diagrams show the center of gravity CG (with distances to axles a and b), the center of roll C (located at distance h from CG), the point/center of primary impact A (with coordinates xA, yA and zA), suspended ms, unsuspended mass mn, total suspension stiffness Ks, total suspension damping (Ds), steering angle δ, vehicle track B.
Figure 4 The four-degree freedom model of vehicle dynamics [6].

The diagrams also show the longitudinal forces at the wheels $F_{x,i}$, the lateral forces at the wheels $F_{y,i}$ (for wheels: index $f$ - front, index $r$ - rear, index $L$ - left, index $R$ - right), the vertical forces on the left axles $F_{z,L}$ and right $F_{z,R}$, as well as the weight forces of the suspended mass $m_g$ and the unsuspended mass $m_{ng}$ (car mass $m = m_g + m_{ng}$). Considering the impact in the horizontal plane, the impact forces $F_{x,\text{impact}}$ and $F_{y,\text{impact}}$ were also reproduced. Regarding the 4 degrees of freedom of the mathematical model, the diagrams highlight the linear velocities (longitudinal $v_x$ and lateral $v_y$), as well as the angular velocities (yaw $\omega_z$ and rollover $\omega_x$ (rollover angle $\phi$)).

The mathematical model with 4 degrees of freedom related to figure 4 consists of four nonlinear first order differential equations, as follows [6]:

- for longitudinal dynamics / motion (unknown $v_x$):

$$m \left( v_x' - v_x \omega_z \right) = F_{x,\text{impact}} + \left( F_{x,f_x} + F_{x,r_x} \right) \cos \delta - \left( F_{y,f_x} + F_{y,r_x} \right) \sin \delta + \left( F_{x,f_x} + F_{x,r_x} \right)$$

(1)

- for lateral dynamics / movement (unknown $v_y$):

$$m \left( v_y' + v_y \omega_x \right) - m_h \omega_x' = F_{y,\text{impact}} + \left( F_{y,f_y} + F_{y,r_y} \right) + \left( F_{x,f_x} + F_{x,r_x} \right) \sin \delta + \left( F_{y,f_y} + F_{y,r_y} \right) \cos \delta$$

(2)

- for rotational motion (unknown $\omega_z$):

$$I_{zz} \omega_z' + I_{xz} \omega_x' = v_x F_{y,\text{impact}} - v_y F_{x,\text{impact}} + F_{x,f_x} + F_{x,r_x} \sin \delta + a \left( F_{y,f_y} + F_{y,r_y} \right) \cos \delta - ...$$

$$- b \left( F_{y,f_y} + F_{y,r_y} \right) + 0.5B \left( F_{x,f_x} - F_{x,r_x} \right) + 0.5B \left( F_{y,f_y} - F_{y,r_y} \right) \cos \delta - \left( F_{y,f_y} - F_{y,r_y} \right) \sin \delta$$

(3)

- for rollover motion (unknown $\omega_x$):

$$I_{xz} \omega_x' + I_{xx} \omega_x' - m_h \left( v_y' + v_y \omega_x \right) = F_{y,\text{impact}} \left( z_A - h \right) + \left( m_{ng} g - K_j \right) \phi - D \omega_x$$

(4)

In these relations also intervene the moments of inertia related to the rotational movements around the respective axes (for example $I_{zz}$ is the moment of inertia of rotation, $I_{xz}$ is the moment of inertia of rollover of the suspended mass etc.), which can be established with relations from specialty literature. The longitudinal forces at the wheels and the lateral forces at the wheels can be established with Pacejka’s relations. The total stiffness and damping of the suspension shall
be determined taking into account that the springs and dampers of the vehicle are arranged in series. Geometric elements and masses are known for a particular vehicle. The coordinates of the center of gravity are established with the relations in the specialized literature.

Considering a triangular-shaped impulse shape (with a peak in the middle of the impact duration $T$), the impact forces on the two directions in figure 4 result:

$$F_{x,impulse} = \frac{2P_x}{T} ; \quad F_{y,impulse} = \frac{2P_y}{T} \quad (5)$$

In expressions (5), $P_x$ and $P_y$ are the percussions on the two axes in the horizontal plane. These are established from the equations on the two axes of the principle of conservation of momentum and result:

$$P_x = \left( m_1 + m_2 \right) (V_x - v_1) ; \quad P_y = \left( m_1 + m_2 \right) (V_y - v_2) \quad (6)$$

where $m_1$ and $m_2$ are the masses of the impact vehicles, $v_1$ and $v_2$ the impact speeds, $V$ the common separation speed, in expressions (6) being the axle components of the speeds.

Having thus the values of the impact forces from the relations (5), according to figure 4, the mathematical model with 4 degrees of freedom is further applied and the desired value of the angular speed of rotation $\omega_{zd}$ results. The Ackermann steering angle is obtained as follows:

$$\delta = \left( \frac{a + b}{v_x} + k_x v_x \right) \omega_{zd} \quad (7)$$

wherein the coefficient of survival $k_u$ has the expression from the ESC system:

$$k_u = \frac{m}{a + b} \left( \frac{b}{C_{a,f}} - \frac{a}{C_{a,s}} \right) \quad (8)$$

where $C_{a,f}$ and $C_{a,s}$ are the side stiffnesses of the front and rear tires.

Expression (7) determines the optimal steering angle, which ensures that a secondary collision is avoided after a primary impact has occurred.

4. Dynamics of vehicles involved in a road accident

It is still aimed at a real road accident in operation, which presents the main elements related to its reconstruction, after which the dynamics of vehicles in the situation of using post-impact displacement control systems are analyzed. The Honda Jazz car and the Mitsubishi Diamante car were involved in this accident, for which in figure 5 some positions of the cars obtained from the reconstruction of the accident with the PC-Crash program are presented. Figure 5 shows that in the final position the Mitsubishi car hit the wall on the side of the road [2, 11, 13, 14].
Figure 5 Road crash scene with multiple collisions.

Figure 6 shows the variation of the speeds of the two cars, as well as some parameters related to the collision between them, which is the primary impact of the road accident in the case without a post-impact control system. The speeds of the cars in the initial position were $v_{i1}=65$ km/h at Honda and $v_{i2}=45$ km/h at Mitsubishi. It also results that the impact between cars was at $t=1.82$ s, at which the impact speeds were $v_1=46.6$ km/h and $v_2=29.2$ km/h.

![Travel speeds of the two cars and some impact parameters, Honda and Mitsubishi, without post-impact stability control system](image)

**Figure 6** Travel speeds of the two cars and some impact parameters.

At this first impact (shown in figure 7) the separation speeds are $V_1=35.1$ km/h and $V_2=22.3$ km/h, values presented in the impact diagram. Figure 6 also shows that following the impact between cars, their maximum deformations (on the main direction of force) were $x_1=18$ cm and $x_2=15$ cm, respectively. The deformation energies were $E_{d1}=30.68$ kJ and $E_{d2}=26.96$ kJ, respectively. Delta-$V$, which indicates the severity of the impact, were $\Delta V_1=14.96$ km/h and $\Delta V_2=10.37$ km/h. The restitution coefficient is $\varepsilon=0.15$, and the tangential friction coefficient $\mu=0.55$. 
Figure 7 The first impact of the accident, between the two cars.

Figure 6 also shows the secondary impact at time $t = 3.82$ s shown in Figure 8, when the Mitsubishi car hit the wall at a speed of 4.2 km/h and stopped.

Figure 8 The second impact of the accident, between the Mitsubishi car and the wall.

It is still considered that the Mitsubishi car has a post-impact control system with solution 1 previously shown, so with the possibility of avoiding the impact with the wall by an additional braking (MCB system: Multi-Collision Brake).

The graph in figure 9 is thus obtained with the speeds for this case, from which the absence of the secondary collision with the wall is ascertained, the Mitsubishi car stopping in front of it at time $t = 4.08$ s, aspect confirmed also in detail A.

The stopping of the Mitsubishi car in front of the wall is also confirmed in figure 10, where it is found that the car stopped at a distance of 0.54 m from the wall at time $t = 4.08$ s; in figure 10a there is a representation in the plane, and in figure 10b a representation in space.
5. Conclusion

The post-impact dynamics control system is of great importance, as an impermissible deviation of the trajectory after a first impact can lead to road accidents with serious consequences for people and significant damage to the vehicles involved. For this reason, the control and stability of the post-impact dynamics concern aspects related to the vehicle, the road and the driver.

Of the four possible solutions to be used by the post-impact control system, the most widely used is to avoid further collisions by additional braking. Of all four solutions, the rapid response of the post-impact control system is of major importance.
References


